Ettd, 1882	P.R.Government College (Autonomous) KAKINADA	Program&Semester IIB.Sc. (IIISem)				
Course Code MAT-301/3201	TITLEOFTHECOURSE  Abstract Algebra					
Teaching	HoursAllocated:60( <b>Theory</b> )	L	Т	P	С	
Pre-requisites:	Basic Mathematics Knowledge on sets and number system.	5	1	-	5	

## Course Objectives:

To provide the learner with the skills, knowledge and competencies to carry out their duties and responsibilities in pure Mathematic environment.

### CourseOutcomes:

On Completion of the course, the students will be able to-						
CO1	Acquire the basic knowledge and structure of groups, subgroups and cyclic					
	groups.					
CO2	Get the significance of the notation of a normal subgroups.					
CO3	Understand the ring theory concepts with the help of knowledge in group theory and					
	to prove thetheorems.					
CO4	Study the homomorphisms and isomorphisms with applications.					

## Course with focus on employability/entrepreneurship /Skill Development modules

Skill Development	Employability			Entrepreneurship	
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UNIT I: (12 Hours)

**GROUPS**: Binary Operation – Algebraic structure – semi group-monoid – Group definition and elementary properties Finite and Infinite groups – examples – order of a group, Composition tables with examples.

UNIT II: (12 Hours)

**SUBGROUPS**:Complex Definition – Multiplication of two complexes Inverse of a complex-Subgroup definition- examples-criterion for a complex to be a subgroups. Criterion for the

product of two subgroups to be a subgroup-union and Intersection of subgroups. **Co-sets and Lagrange's Theorem:** Cosets Definition-properties of Cosets–Index of a subgroups of a finite groups–Lagrange's Theorem.

UNIT III: (12 Hours)

**NORMAL SUBGROUPS**: Definition of normal subgroup – proper and improper normal subgroup – Hamilton group – criterion for a subgroup to be a normal subgroup – intersection of two normal subgroups – Sub group of index 2 is a normal sub group –quotient group – criteria for the existence of a quotient group.

**HOMOMORPHISM**: Definition of homomorphism – Image of homomorphism elementary properties of homomorphism – Isomorphism – automorphism definitions and elementary properties—kernel of a homomorphism – fundamental theorem on Homomorphism and applications.

UNIT IV: (12 Hours)

**PERMUTATIONS:** Definition of permutation – permutation multiplication – Inverse of a permutation – cyclic permutations – transposition – even and odd permutations – Cayley's theorem.

UNIT V: (12 Hours)

#### RINGS

Definition of Ring and basic properties, Boolean Rings, divisors of zero and cancellation laws Rings, Integral Domains, Division Ring and Fields, The characteristic of a ring - The characteristic of an Integral Domain, The characteristic of a Field. Sub Rings.

## Co-Curricular Activities (15 Hours)

Seminar/ Quiz/ Assignments/ Group theory and its applications / Problem Solving.

## TEXT BOOK :

1. A text book of Mathematics for B.A. / B.Sc. by B.V.S.S. SARMA and others, published by S.Chand & Company, New Delhi.

#### **REFERENCE BOOKS:**

- 1. Abstract Algebra by J.B. Fraleigh, Published by Narosa publishing house.
- 2. Modern Algebra by M.L. Khanna.
- 3. Rings and Linear Algebra by Pundir & Pundir, published by Pragathi Prakashan.

### Additional Inputs;

Cyclic Groups, Maximal Ideals and Prime Ideals.

## CO-POMapping:

(1:Slight[Low]; 2:Moderate[Medium]; 3:Substantial[High], '-':NoCorrelation)

	P01	P02	P03	P04	P05	P06	P07	P08	P09	P010	PSO1	PSO2	PSO3
CO1	3	3	2	3	3	3	1	2	2	3	2	3	2
CO2	3	2	3	3	2	3	3	1	3	3	3	2	1
CO3	2	3	2	3	2	3	2	2	2	3	2	2	3
CO4	3	2	3	2	2	2	3	3	1	1	3	1	2

## BLUE PRINT FOR QUESTION PAPER PATTERN

## **SEMESTER-III**

Unit	TOPIC	S.A.Q	E.Q	Marks allotted to the Unit
I	Groups	2	1	20
II	Subgroups , Co-sets and Lagrange's Theorem	2	1	20
III	Normal subgroups, Homomorphism	1	2	25
IV	Permutations.	1	1	15
V	Rings	1	1	15
	Total	7	6	95

**S.A.Q.** = Short answer questions (5 marks)

**E.Q** = Essay questions (10 marks)

Short answer questions  $: 4 \times 5 = 20 \text{ M}$ 

Essay questions  $: 3 \times 10 = 30 \text{ M}$ 

Total Marks = 50 M

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# P.R. Government College (Autonomous), Kakinada II year B.Sc., Degree Examinations - III Semester Mathematics Course: Abstract Algebra Paper III (Model Paper w.e.f. 2021-22)

Time: 2Hrs Max. Marks: 50

### PART - I

Answer any FOUR questions. Each question carries FIVE marks.

4 X 5 M=20 M

- **1.** Prove that in a group  $G(\neq \emptyset)$ , for  $a, b, x, y \in G$ , the equations  $ax = b, ya = b, \forall a, b \in G$  have unique solutions.
- **2.** If G is a group, for  $a, b \in G$  prove that  $(ab)^{-1} = b^{-1}a^{-1}$
- **3.** If a non empty complex H of a group G is a subgroup of G then prove that  $H = H^{-1}$ .
- **4.** If G is a finite group and  $a \in G$  then show that O(a) divides O(G).
- **5.** Define Normal subgroup. Prove that a subgroup H of a Group (G,.) is a normal subgroup of G if and only if  $xHx^{-1} = H \ \forall \ x \in G$ .
- **6.** Express the product (2 5 4)(1 4 3)(2 1) as a product of disjoint cycles and find its inverse.
- 7. Prove that the characteristic of an integral domain is either a prime or zero.

#### PART - II

Answer Any THREE questions. Each question carries Ten marks. 3 X 10 M = 30 M

- 9. A finite semi –Group (G, ·) satisfying the cancellation laws is a group.
- 10. Prove that a non empty complex H of a group G is a subgroup of G if and only if

$$a, b \in H \Rightarrow ab^{-1} \in H$$
.

- 11. If H is a normal subgroup of a group (G,.) then prove that the product of two right (or) left cosets of H is also a right (or) left coset of H in G.
- 12. State and prove fundamental theorem on homomorphisms of groups.
- 13. State and prove Cayley's theorem.
- 14. Prove that the ring of integers Z is a principal ideal ring.